

# GCSE MATHEMATICS 8300/1H

Higher Tier Paper 1 Non-Calculator

Mark scheme

June 2020

Version: 1.0 Final



Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aga.org.uk

### Copyright information

AQA retains the copyright on all its publications. However, registered schools/colleges for AQA are permitted to copy material from this booklet for their own internal use, with the following important exception: AQA cannot give permission to schools/colleges to photocopy any material that is acknowledged to a third party even for internal use within the centre.

Copyright © 2020 AQA and its licensors. All rights reserved.

# **Glossary for Mark Schemes**

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

M	Method marks are awarded for a correct method which could lead to a correct answer.
A	Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
В	Marks awarded independent of method.
ft	Follow through marks. Marks awarded for correct working following a mistake in an earlier step.
sc	Special case. Marks awarded for a common misinterpretation which has some mathematical worth.
M dep	A method mark dependent on a previous method mark being awarded.
B dep	A mark that can only be awarded if a previous independent mark has been awarded.
oe	Or equivalent. Accept answers that are equivalent.
	eg accept 0.5 as well as $\frac{1}{2}$
[a, b]	Accept values between a and b inclusive.
[a, b)	Accept values a
3.14	Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416
Use of brackets	It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles.

# **Diagrams**

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

## Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

# Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

### Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

# Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

### **Further work**

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

### Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

## Work not replaced

Erased or crossed out work that is still legible should be marked.

# Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

# Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

### Continental notation

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the student intended it to be a decimal point.

Q	Answer	Mark	Comments
1	<u>19</u> 4	B1	

Q	Answer	Mark	Comments
2	$\begin{pmatrix} 3 \\ -2 \end{pmatrix}$	B1	

Q	Answer	Mark	Comments
3	1 000 000	B1	

Q	Answer	Mark	Comments
4	<u>6</u> 5	B1	

Q	Answer	Mark	Comments	
	Alternative method 1			
	cos and $\frac{9}{18}$ oe identified	M1		
	60	A1		
	Alternative method 2			
5	sin and $\frac{\sqrt{18^2 - 9^2}}{18}$ identified or tan and $\frac{\sqrt{18^2 - 9^2}}{9}$ identified	M1		
	60	A1		
	Additional Guidance			
	Accept an embedded answer, eg cos	$60 = \frac{9}{18}$	with no further working	M1A1
	180 ÷ 3 = 60			M0A0

Q	Answer	Mark	Comments		
	Graph A Strong negative	B1			
	Graph B No correlation	B1	allow 'No' or 'None'		
6	Additional Guidance				
	Condone incorrect spelling if intention is clear				
	Allow clear link(s) from the table to the answer line eg an arrow from 'Strong negative' to the Graph A answer line				

	Answer	Mark	Commer	nts
	12 in correct position	B1		
	24 in correct position	B1		
	11 in correct position or 33 in correct position or their value in G only is three times their value in the intersection or their four values sum to 80	B1ft	ft $\frac{1}{4}$ × (80 – 12 – their 24)  ft $\frac{3}{4}$ × (80 – 12 – their 24)  for this mark allow non-integers or values rounded or truncated to the nearest integer	
7	12, 24, 11 and 33 in correct positions	B1		
	Additional Guidance			
	Mark the Venn diagram only			
	ξ S G G 12 11 33 24		B1B1B1B1	

Q	Answer	Mark	Commen	ts	
	Alternative method 1				
	6.5 × 9 or 58.5 or 6.5 × 7 or 45.5	M1	oe		
	$\frac{6.5 \times 9 - 2 \times 6.5}{2} \text{ or } \frac{58.5 - 13}{2}$ or $\frac{6.5 \times 7}{2}$ or $\frac{45.5}{2}$	M1dep	oe division may be implied eg $\frac{7}{9}$ = 45.5, $\frac{3.5}{9}$ = 22.3	25 scores M1M1	
	22.75 or $\frac{91}{4}$ or $22\frac{3}{4}$	A1	oe		
8	Alternative method 2				
	6.5 × 9 or 58.5 or 6.5 × 4.5 or 29.25	M1	oe		
	$\frac{6.5 \times 9}{2} - 6.5$ or $6.5 \times 4.5 - 6.5$	M1dep	oe eg 6.5 × (4.5 – 1) or	6.5 × 3.5	
	22.75 or $\frac{91}{4}$ or $22\frac{3}{4}$	A1	oe		
	Ad	ditional G	Buidance		
	Answer 22.8 or 23 with 22.75 in working			M1M1A1	
	Answer 22.8 or 23 without 22.75 in w	orking		A0	

Q	Answer	Mark	Commer	nts
	First term 2 and Third term 8	B2	B1 one correct or First term $2^1$ or Third term $2^3$ or First term $-2$ and T or $4x^2 = 16$ (any letter) or $ar = 4$ and $ar^3 = 16$	
	Add	ditional G	Buidance	
	If answer lines are blank, mark progre	ession firs	t and then working lines	
9(a)	Correct answer for 1st term or 3rd ter numerical term on answer line	m in the p	progression, but incorrect	B0 for that term
	Correct answer for 1st term or 3rd term in the progression, with non-contradictory algebraic term on answer line			B1 for that term
	Correct answers for 1st term and 3rd term in the progression, with non contradictory algebraic terms on answer lines			B2
	First term 2 Third term 2 <sup>3</sup>		B1	
	First term -2 Third term 10			В0
	$4x = \frac{16}{x}$ (any letter)			B1

Q	Answer	Mark	Commer	nts	
	Alternative method 1	-			
	3rd term = $9p$	M1	oe implied by a total of $15p$		
	p + 5p + their 3rd term = 90 or $15p = 90$	M1	oe their 3rd term must be expression in terms of $p$ 90 ÷ 15 implies M1M1		
	6	A1ft	ft their 3rd term, which must be a linear expression in $p$ , or their equation in the form sum of 3 linear terms in $p=90$		
			allow ft answers rounde	d to 1dp or better	
	Alternative method 2	T			
	90 ÷ 3 or 30	M1	oe		
	5p = their $30$	M1dep	oe		
	6	A1			
	Additional Guidance				
9(b)	For A1ft, if not an integer, the answer must be given as a decimal, fully simplified fraction or fully simplified mixed number				
	Once awarded, ignore further incorre				
	eg $p + 5p + 25p = 90$ , $31p = 90$ , $p = \frac{90}{31}$ , $p = 3$ (ignore conversion)			M0M1A1ft	
	Their 3rd term may first appear in their addition, eg $p+5p+10p=90$ implies that $10p$ is their 3rd term			M0M1	
	(3rd term $5p + 4$ ), $p + 5p + 5p + 4 = 90$ , $p = 7.8$			M0M1A1ft	
	(3rd term $10p$ ), $p + 5p + 10p = 90$ , $p = 5.625$			M0M1A1ft	
	Sum 15p and/or answer 6 may come				
	eg1 (3rd term $10p$ ), $p + 5p + 10p = 15p$ , ( $15p = 90$ ), $p = 6$ receives 2nd mark only; they have an incorrect 3rd term and an incorrect total for their 3 terms, but their answer is correct for their total, so equating to 90 is implied even if not seen			M0M1A0ft	
	eg2 (3rd term 10 $p$ ), $p$ , 5 $p$ , 10 $p$ , 15 $p$ = 90, $p$ = 6			M0M0A0ft	
	If their 3rd term has an algebraic coefficient the 2nd mark can be awarded for a correct equation, but A1 cannot be awarded				
	eg (3rd term $np$ ), $p + 5p + np = 90$			M0M1A0	

Q	Answer	Mark	Commen	ts		
	Alternative method 1					
	2400 ÷ (3 + 5) or 2400 ÷ 8 or 300	M1	oe accept $\frac{1}{8}$ of 2400			
	5 × their 300 or 1500 or 3 × their 300 or 900 or their 300 ÷ 6 or 50	M1dep	oe			
	5 × their 300 ÷ 6 or (2400 – 3 × their 300) ÷ 6 or 1500 ÷ 6	M1dep	oe			
10	250	A1				
	Alternative method 2					
	2400 ÷ 6 or 400	M1	oe			
	their 400 ÷ (3 + 5) or 50	M1dep	oe 2400 ÷ 48 scores M	1M1		
	5 × their 50 or 400 – (3 × their 50)	M1dep	oe			
	250	A1				
	Ad					
	Answer 400 with 1500 or 900 in work	M1M1M0A0				
	Answer 400 with 250 in working	M1M1M1A0				
	Condone incorrect representation of a division if recovered eg 8 ÷ 2400 = 300			M1		

Q	Answer	Mark	Comments		
	Alternative method 1				
	0.275 × 3 or 0.825		oe		
	or	M1			
	0.275 ÷ 10 or 0.0275				
	0.0825	A1			
	Alternative method 2				
	0.08 from division of 33 by 400				
	or	M1			
	0.08 from division of 3.3 by 40				
11	0.0825	A1			
	Alternative method 3				
	33 × 1000		oe		
	400				
	or 33 × 2.5				
	or 33 ÷ 4	M1			
	or	IVI I			
	0.33 ÷ 4				
	or				
	digits 825				
	0.0825	A1			

Q	Answer	Mark	Commer	nts
	$21 \div 7 \times 2 (= 6)$ or $21 \div 3 = 7$ and $6 \div 3 = 2$ or $21 \div 7 = 3$ and $6 \div 2 = 3$ or $7 \times 3 = 21$ and $2 \times 3 = 6$	B1	oe eg 6 ÷ 2 = 3 and 7	× 3 = 21
	Additional Guidance			
	3 × 2 (= 6)			В0
12(a)	7 : 2 (=) 21 : 6 with no other working			В0
	7 : 2 (=) 21 : 6 with multiplication by 3 shown by arrow(s)			B1
	7:2(=)14:4(=)21:6			B1
	Do not condone incorrect representat	ion of a di	vision eg 7 ÷ 21 = 3	В0
	Do not condone incorrect mathematic	entation	В0	
	eg 21 ÷ 7 = 3 × 2 = 6			_
	$21 \div 6 = 3.5, 3.5 \times 2 = 7$			B1
	$21 \times 2 = 42, 42 \div 7 = 6$			B1

Q	Answer	Mark	Comments		
	Alternative method 1				
	$2 \times \pi \times 21$ or $\pi \times 42$ or $42\pi$ or $[131.88, 132]$	M1	oe condone [3.14, 3.142] for $\pi$		
	$2 \times \pi \times 6 \div 4$ or $\pi \times 12 \div 4$ or $3\pi$ or $[9.4, 9.43]$	M1	oe arc length of quarter circle condone [3.14, 3.142] for $\pi$		
	$2 \times \pi \times 6 \div 4 + 2 \times 6$ or $3\pi + 12$ or [21.4, 21.43]	M1dep	oe dep on 2nd M1 this does not imply M1M1M1		
	45π + 12	A1			
12(b)	Alternative method 2				
	$2 \times \pi \times 21$ or $\pi \times 42$ or $42\pi$ or $[131.88, 132]$	M1	oe condone [3.14, 3.142] for $\pi$		
	$2 \times \pi \times 21$ and $2 \times \pi \times 6 \div 4$ or $42\pi$ and $3\pi$ or $2 \times \pi \times 21 + 2 \times 6$ or $42\pi + 12$ or $[143.88, 144]$	M1dep	oe eg 42π and [9.4, 9.43] or [131.88, 132] and 3π		
	$2 \times \pi \times 21 + 2 \times \pi \times 6 \div 4$ or $42\pi + 3\pi$ or $45\pi$ or [141, 141.43] or [153, 153.43]	M1dep	oe $eg \ 42\pi + [9.4, 9.43]$ or [131.88, 132] + $3\pi$		
	45π + 12	A1			

# Additional guidance for this question is on the next page

	Additional Guidance				
	Condone $3(15\pi + 4)$	M1M1M1A1			
	Condone, for example, π42 for up to M1M1M1				
	$21\pi + 3\pi + 12$	M0M1M1A0 on alt 1			
12(b) cont	$441\pi + 3\pi + 12$	M0M1M1A0 on alt 1			
	$42\pi + 36\pi + 12$	M1M1M0A0 on alt 2			
	$441\pi + 36\pi + 12$	МОМОМОАО			
	Using $\pi r^2$ instead of $2\pi r$ throughout	M0M0M0A0			
	$45\pi + 12$ in working with incorrect further work, eg $45\pi + 12 = 57\pi$	M1M1M1A0			

Q	Answer	Mark	Commen	its
13(a)	(x+8)(x-5) or $(k=) 3or (x+5)(x-8) or (k=) -3or (x+10)(x-4) or (k=) 6or (x+4)(x-10) or (k=) -6or (x+20)(x-2) or (k=) 18or (x+2)(x-20) or (k=) -18or (x+40)(x-1) or (k=) 39or (x+1)(x-40) or (k=) -39or s=8 and t=5or 8-5$	M1	oe correct factorisation	
	3	A1	condone embedded ans	wer $x^2 + 3x - 40$
	Additional Guidance			
	$x^2 + sx - tx - st$ with no further working		M0A0	
	Ignore incorrect factorisations in working	ng		

Q	Answer	Mark	Commen	ts	
	Valid reason	B1	eg it should be $-2$ or $4 \times -5$ isn't 0 or (2+2)(2-7) = -20 or 2+2=4 or $2+2 \neq 0$		
13(b)	Additional Guidance				
	'He didn't change the sign on the left'			B1	
	'If you substitute 2 it does not give 0'			B1	
	x = 2 is wrong			B1	
	x = -2 (and $x = 7$ )			B1	
	x = -2 and $x = -7$			В0	
	'One solution is wrong' or 'Only one answer is correct'			В0	
	x = 2			В0	
	Ignore statements which do not contr	adict a co	orrect answer		

Q	Answer	Mark	Commen	ts
	$(18 =) 2 \times 3^2$ or $(18 =) 2 \times 3 \times 3$	M1	oe eg (18 =) $2^1 \times 3^1 \times 3$ allow 2, 3 and 3 in a factor	
	$2^{11}\times3^3\times5^6$	A1	any order SC1 864 000 000	
	Additional Guidance			
14(0)	M1 may be implied eg1 $2 \times 3^2 \times 2^{10} \times 3 \times 5^6$		M1	
14(a)	eg2 $2^{11} \times 3 \times 3 \times 3 \times 5^6$			M1
	Condone a multiplier of 1 for M1 only	if not rec	overed	
	eg1 $1 \times 2 \times 3 \times 3$			M1
	eg2 $1 \times 2^{11} \times 3^3 \times 5^6$		M1A0	
	Allow the prime factorisation of 18 with larger number	thin the pi	rime factorisation of a	
	eg $54 \times 2^{10} \times 5^6$ and $54 = 2 \times 3^3$ oe			M1

Q	Answer	Mark	Comments
14(b)	$\sqrt[3]{2^6 \times 11^3}$ or $\sqrt[3]{64 \times 11^3}$ or $2^2 \times 11$ or $4 \times 11$ or $3\sqrt[3]{85184}$	M1	oe with no fraction in the surd eg $\sqrt[3]{64 \times 1331}$ oe eg $2^{(6 \div 3)} \times 11^{(3 \div 3)}$ or $2^1 \times 2^1 \times 11^1$
	44	A1	

Q	Answer	Mark	Comments
15	1:6	B1	

Q	Answer	Mark	Commen	ts	
	0.5	B1	oe		
	-8	B1ft	ft any value other than 1		
	Ado				
	If they show $u_2 = \frac{4}{8}$ but simplify or convert it incorrectly, award B1 for the 1st mark, but do not award B1(ft) for the 2nd mark				
16	eg $u_2 = \frac{4}{8} = \frac{1}{4}$ , $u_3 = \frac{4}{-0.75} = -\frac{16}{3}$		B1B0		
	0.5 (oe) and –8 worked out, with –8 c	nswer line	B0B1		
	Non-integer answers must be given as correct decimals or correct fractions with integer numerator and denominator  If ft, award the 2nd mark for a correct fraction with integer numerator				
	and denominator even if then incorrectly simplified or converted				
	If the answer line for $u_2$ is incorrect, d $10 = \frac{4}{8}$ in working	o not awa	rd the 1st mark for		

Q	Answer	Mark	Commer	nts
	h = 3n + 20 or h = 20 + 3n	В3	oe in the form $h = $ B2 correct equation not or $3n + 20$ or $20 + 3n$ or $h = 3n \ (+k) \ (k \text{ is a n or } h = (k+) 3n \ (k \text{ is a n or } h = an + 20 \ (a \neq 0)$ or $h = 20 + an \ (a \neq 0)$ B1 $3n \ (+k) \ (k \text{ is a number or } (k+) 3n \ (k \text{ is a number or } (k+) 3n \ (k \text{ is a number or } (k+) 3n \ (k \text{ is a number or } (k+) 3n \ (k \text{ is a number or } (k+) 3n \ (k \text{ is a number or } (k+) 3n \ (k \text{ is a number or } (k+) 3n \ (k+)$	umber or letter) umber or letter) nber or letter)
	Additional Guidance			
17	Allow $h$ = in working but omitted on answer line For an equation in the form $h$ = in working, but rearranged (correctly or incorrectly) for the answer line, award 1 mark less than the $h$ = form			
	Condone an unsimplified fraction for denominator $eg h = \frac{12}{4}n + 20$	3 if it has	integer numerator and	В3
	An unsimplified fraction for 3 can still integer numerator and denominator	score ma	rks if it does not have	
	eg $h = \frac{32-20}{4}n+20$			B2
	Allow $3 \times n$ or $n \times 3$ for $3n$			
	Ignore units			
	Condone capital $H$ or $N$ , but for incorthan correct variable(s) would get	rect varial	ole(s) award 1 mark less	
	eg1 $h = 3x + 20$ or $y = 3x + 20$			B2
	eg2 $3x + 20$ eg3 $3x$			B1 B0

Q	Answer	Mark	Comments
	Alternative method 1: substitutes t	for 4y in f	irst equation then substitutes value of <i>x</i>
	2x + 2(4x - 7) = -9 or $10x = 5$	M1	oe correct elimination of y
	$(x =) \frac{1}{2}$ or $(x =) 0.5$	A1	oe eg $(x =) \frac{5}{10}$
	$2 \times \text{their } \frac{1}{2} + 4y = -9$ or	M1dep	oe substitution of their $\boldsymbol{x}$ into either equation
	$2y = 4 \times \text{their } \frac{1}{2} - 7$	Wildep	
	$(y =) -\frac{5}{2}$ or $(y =) -2\frac{1}{2}$ or $(y =) -2.5$	A1	oe eg $(y =) -\frac{10}{4}$
18	Alternative method 2: equates coe	fficients	
	_	Incients	
	Equates coefficients for one unknown and if necessary, rearranges into appropriate form	M1	eg 1 changes 1st equation to $4x + 8y = -18$ , rearranges 2nd equation to $2y - 4x = -7$ and adds to eliminate $x$ eg 2
	and adds or subtracts equations appropriately		changes 2nd equation to $4y = 8x - 14$ and subtracts to eliminate $y$
	Correct value for <i>x</i> or <i>y</i>	A1	
	Substitutes their value into an equation	M1dep	
	Both values correct	A1	

Mark scheme and Additional Guidance continues on next page

Q	Answer	Mark	Commer	nts		
	Alternative method 3: substitutes for $4x$ in second equation then substitutes value of $y$					
	2y = 2(-9 - 4y) - 7 or $10y = -25$	M1	oe correct elimination of	X		
	$(y =) -\frac{5}{2}$ or $(y =) -2\frac{1}{2}$	A1	oe eg $(y =) -\frac{25}{10}$			
	or $(y =) -2.5$ $2x + 4 \times \text{their } -\frac{5}{2} = -9$		oe substitution of their $y$ equation	into either		
	or $2 \times \text{their} -\frac{5}{2} = 4x - 7$	M1dep				
	$(x =) \frac{1}{2}$ or $(x =) 0.5$	A1	oe eg ( $x = \frac{2}{4}$			
18 cont	Alternative method 4: solves each unknown separately - substitutes for $4y$ in first equation then substitutes for $4x$ in second equation					
	2x + 2(4x - 7) = -9 or $10x = 5$	M1	oe correct elimination of $y$			
	$(x =) \frac{1}{2}$ or $(x =) 0.5$	A1	oe eg ( $x = $ ) $\frac{5}{10}$			
	2y = 2(-9 - 4y) - 7 or $10y = -25$	M1	oe elimination of x			
	$(y =) -\frac{5}{2}$ or $(y =) -2\frac{1}{2}$	A1	oe eg $(y =) -\frac{25}{10}$			
	or $(y =) -2.5$					
	Additional Guidance					
	Note that in alt 4 the 2nd M mark is not dependent					
	In alt 4, allow alt 2 method for each u	ınknown				
	Both answers correct			M1A1M1A1		

Q	Answer	Mark	Comments
19	$\frac{3x}{10}$	B1	

Q	Answer	Mark	Comments
20(a)	1	B1	

Q	Answer	Mark	Comments
	$\frac{1}{8}$ or 0.125		B1 correct expression including at least one of
			changes 32 to 2 <sup>5</sup>
20(b)		B2	shows that the negative index means the reciprocal
			shows that index $\frac{1}{5}$ means 5th root
			splits the index into the multiplication of two indices

Q	Answer	Mark	Comments	
21	Smallest $3\sqrt{23}$ 15.6 $\frac{47}{3}$ Largest $2.1^4$	B2	B1 three values in correct order if the other value were removed eg Smallest $3\sqrt{23}$ $2.1^4$ $15.6$ Largest $\frac{47}{3}$	
	Additional Guidance			
	Mark the answer only			
	Accept equivalent values used on answer lines			

Q	Answer	Mark	Comments
	$y = kx^3$ or $17 = 4^3k$	M1	oe
	$k = 17 \div 4^3$		oe in the form $k =$
	or $k = 17 \div 64$		
	or $k = \frac{17}{64}$	M1dep	
	or		
22(a)	$\frac{17}{64}x^3$		
	$y = \frac{17}{64}x^3$ or $y = 0.265625x^3$		oe equation eg $64y = 17x^3$
	64	A1	SC2
			$y = \frac{17}{4^3}x^3$ or $y = \frac{17}{64} \times 4^3$
	Additional Guidance		
	Allow the proportion sign instead of =	for M1 or	nly

Q	Answer	Mark	Comments
22(b)	÷ 2	B1	

Q	Answer	Mark	Comments	
	Alternative method 1: works out the value of $\boldsymbol{x}$ using two different methods and shows they are different			
	Any one of		oe	
	4x + 92 = 180			
	or			
	5x + 30 + x + 36 = 180	M1		
	or $6x + 66 = 180$	IVII		
	or			
	4x + x + 36 + 5x + 30 + 92 = 360			
	or $10x + 158 = 360$			
	(x =) 22 with M1 seen		must be correct value for corresponding	
	or	A1	equation	
	(x =) 19 with M1 seen			
	or			
23	(x =) 20.2 with M1 seen			
	A different one of		oe	
	4x + 92 = 180			
	or			
	5x + 30 + x + 36 = 180	M1		
	or $6x + 66 = 180$	177.1		
	or			
	4x + x + 36 + 5x + 30 + 92 = 360			
	or $10x + 158 = 360$			
	Any two of		must be correct values for corresponding	
	(x =) 22 with M1 seen	A1	equations	
	or $(x =)$ 19 with M1 seen			
	or $(x =) 20.2$ with M1 seen	, , , ,		
	and			
	should be equal		oe statement	

Mark scheme and Additional Guidance continue on the next page

Q	Answer	Mark	Comments	
	Alternative method 2: uses angle sum of quadrilateral to work out $x$ and then shows opposite angles do not sum to 180°			
	4x + x + 36 + 5x + 30 + 92 = 360 or $10x + 158 = 360$	M1	oe	
	(x =) 20.2 with M1 seen	A1		
	4 × their 20.2 + 92		oe	
	or 5 × their 20.2 + 30 + their 20.2 + 36	M1dep		
	$4 \times 20.2 + 92 = 172.8$ and should be 180	A1	oe oe statement	
23	or $5 \times 20.2 + 30 + 20.2 + 36 = 187.2$ and should be 180	AI	oe oe statement	
cont	Alternative method 3: uses angle sum of $4x$ and $92^{\circ}$ to work out $x$ and then shows other angles do not sum to $180^{\circ}$ or all angles do not sum to $360^{\circ}$			
	4x + 92 = 180	M1	oe	
	(x =) 22 with M1 seen	A1		
	$5 \times$ their 22 + 30 + their 22 + 36 or $4 \times$ their 22 + 92 + 5 $\times$ their 22 + 30 + their 22 + 36	M1dep	oe	
	$5 \times 22 + 30 + 22 + 36 = 198$ and should be 180		oe oe statement	
	or 4 × 22 + 92 + 5 × 22 + 30 + 22 + 36 = 378	A1	oe	
	and should be 360		oe statement	

Mark scheme and Additional Guidance continue on the next page

Q	Answer	Mark	Commen	ts	
	Alternative method 4: uses angle sum of $5x + 30$ and $x + 36^{\circ}$ to work out $x$ and then shows other angles do not sum to $180^{\circ}$ or all angles do not sum to $360^{\circ}$				
	5x + 30 + x + 36 = 180 or $6x + 66 = 180$	M1	oe		
	(x =) 19 with M1 seen	A1			
	4 × their 19 + 92 or 5 × their 19 + 30 + their 19 + 36 + 4 × their 19 + 92	M1dep	oe		
23 cont	$4 \times 19 + 92 = 168$ and should be 180 or $5 \times 19 + 30 + 19 + 36 + 4 \times 19 +$ 92 = 348	A1	oe oe statement oe		
	and should be 360		oe statement		
	Additional Guidance				
	Alts 1 and 2 $x = 20.2$ with M1 not seen			Zero	
	Alts 1 and 3 $x = 22$ with M1 not seen			Zero	
	Alts 1 and 4 $x = 19$ with M1 not seen			Zero	
	Allow $20\frac{1}{5}$ or $\frac{101}{5}$ for 20.2, but do not allow other improper fractions for 20.2, 22 or 19 unless recovered				

Q	Answer	Mark	Comments
24	$\sin y > 0$ and $\cos y < 0$	B1	

Q	Answer	Mark	Commen	its
25	5 × 2 or 10 or 10 × 3 or 30 or 5 × 4 or 20	M1	oe may be written on bars	
	$74 - 5 \times 2 - 10 \times 3 - 5 \times 4$ or $74 - 10 - 30 - 20$ or 14	M1dep	oe bar of area 14 implies M	2
	their 14 ÷ 10 or 1.4	M1dep	implied by correct bar fo	r their 14
	Bar drawn from 170, width 10 and height 1.4	A1		
	Additional Guidance			
	Bar from 170 to 175 with height 2.8			M1M1M0A0

Q	Answer	Mark	Comments	
26(a)	$\frac{14}{\sqrt{7}} \times \frac{\sqrt{7}}{\sqrt{7}}$ or $\frac{14\sqrt{7}}{7}$	M1		
	2√7	A1	do not award if further work eg $\sqrt{14}$	
	Additional Guidance			
	Correct answer with no working			M1A1

Q	Answer	Mark	Commen	nts
26(b)	240	B3	B2 any correct single value $a\sqrt{b}$ where $a\geqslant 2$ eg $24\sqrt{100}$ or $12\sqrt{40}$ or $6\sqrt{1600}$ or $2\sqrt{1440}$ or correct product of two or eg $24\times10$ or $8\times30$ or $2\times2\times5\times4\times3$ B1 $(\sqrt{80}=)4\sqrt{5}$ or $(\sqrt{80}=)4\sqrt{5}$	on $\sqrt{900}$ or $\sqrt{900}$ or $\sqrt{900}$ or $\sqrt{900}$ or $\sqrt{18}$
	Additional Guidance			
	$4\sqrt{5} \times 3\sqrt{2} \times 2\sqrt{10}$			B1
	$4\sqrt{5} \times 3\sqrt{2} \times \sqrt{40}$			B1

Q	Answer	Mark	Comments	
	9 : 25	B1	oe ratio	
	3:5	B1	oe ratio allow $\sqrt{9}$ : $\sqrt{25}$	
27	Additional Guidance			
	25 : 9			В0
	5:3			В0
	Answers transposed			B0B0

Q	Answer	Mark	Comments	
	4(6+x)(6-x) or $-4(x+6)(x-6)$	B2	oe with full factorisation B1 $(12+2x)(12-2x)$ or $2(6+x)(12-2x)$ or $(12+2x)2(6-x)$ or $2(6+x)2(6-x)$ or $4(36-x^2)$ oe	
	Additional Guidance			
	$2(72-2x^2)$			В0
28	Condone multiplication signs for B1 or B2			
	eg1 $4 \times (6 + x) \times (6 - x)$			B2
	eg2 $(12+2x) \times (12-2x)$			B1
	eg3 $(12 + 2 \times x) \times (12 - x \times 2)$		B1	
	Condone missing final bracket			
	eg1 $4(6+x)(6-x)$			B2
	eg2 $(12+2x)(12-2x)$		B1	
	Do not allow x2 for 2x			
	Ignore attempts to solve $144 - 4x^2 = 0$			

Q	Answer	Mark	Comments	
	$(x-4)^3$	B1	$(x+4)^3$ is B0	
	$x^2 - 4x - 4x + 16$ with 3 terms correct or $x^2 - 8x + k$ where $k$ is a non-zero constant	M1	ft $(x+4)^3$ only	
29	$x^{3} - 4x^{2} - 4x^{2} + 16x - 4x^{2} + 16x + 16x - 64 (+ 6)$ or $x^{3} - 8x^{2} + 16x - 4x^{2} + 32x - 64 (+ 6)$ or $x^{3} - 12x^{2} + 48x - 64 (+ 6)$	M1dep	oe full expansion of their 4 terms by $(x-4)$ with at least 4 terms correct or full expansion of their 3 terms by $(x-4)$ with at least 3 terms correct ft $(x+4)^3$ only	
		A1	idanaa	
	Additional Guidance			
	Using $(x + 4)^3$ can score a maximum of B0M1M1A0 $x^2 + 4x + 4x + 16$ with 3 terms correct or $x^2 + 8x + k$ where $k$ is a non-zero constant $x^3 + 4x^2 + 4x^2 + 16x + 4x^2 + 16x + 16x + 64$ (+ 6) or $x^3 + 8x^2 + 16x + 4x^2 + 32x + 64$ (+ 6)			B0M1 B0M1M1A0
	or $x^3 + 12x^2 + 48x + 64$ or $x^3 + 12x^2 + 48x + 70$			344444