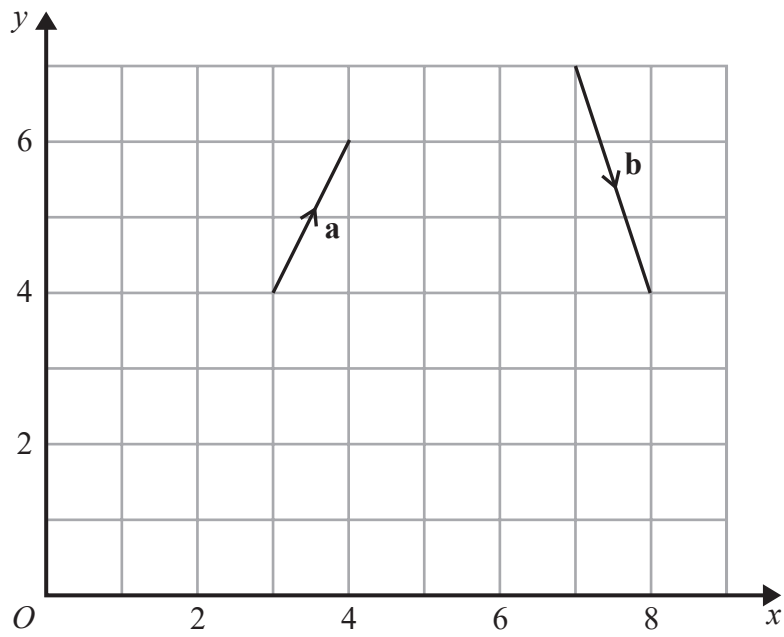


1 The vector \mathbf{a} and the vector \mathbf{b} are shown on the grid.



(a) On the grid, draw and label vector $-2\mathbf{a}$

(1)

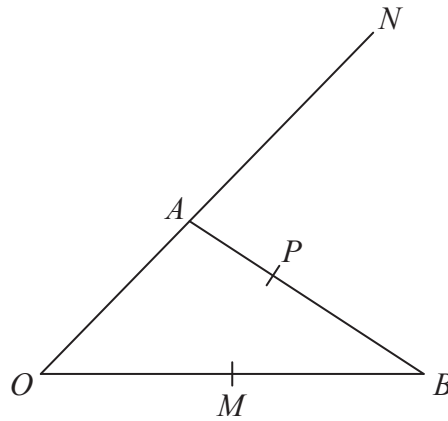
(b) Work out $\mathbf{a} + 2\mathbf{b}$ as a column vector.

$$\begin{pmatrix} \\ \text{---} \\ \end{pmatrix}$$

(2)

(Total for Question 1 is 3 marks)

2



OAN , OMB and APB are straight lines.

$AN = 2OA$.

M is the midpoint of OB .

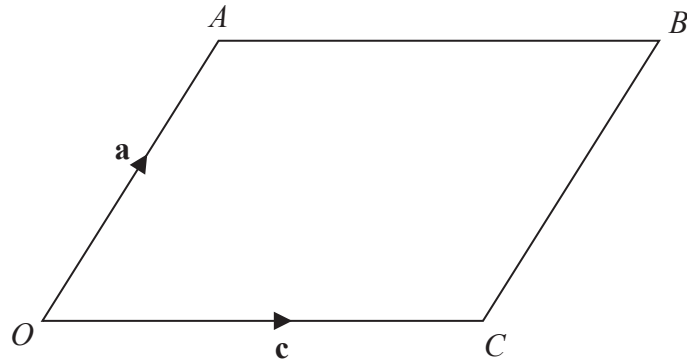
$\vec{OA} = \mathbf{a}$ $\vec{OB} = \mathbf{b}$

$\vec{AP} = k\vec{AB}$ where k is a scalar quantity.

Given that MPN is a straight line, find the value of k .

.....
(Total for Question 2 is 5 marks)

3



$OABC$ is a parallelogram.

$$\vec{OA} = \mathbf{a} \text{ and } \vec{OC} = \mathbf{c}$$

X is the midpoint of the line AC .

OCD is a straight line so that $OC : CD = k : 1$

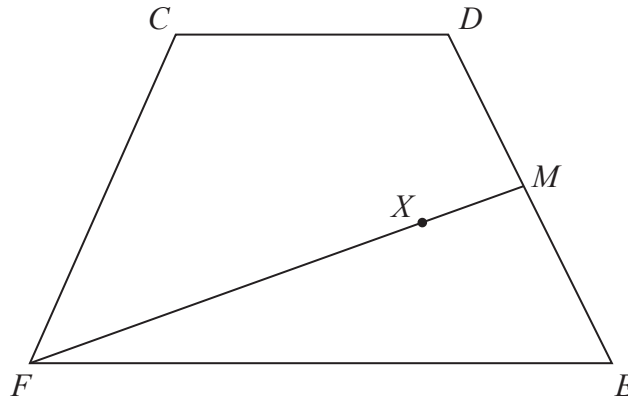
$$\text{Given that } \vec{XD} = 3\mathbf{c} - \frac{1}{2}\mathbf{a}$$

find the value of k .

$$k = \dots\dots\dots$$

(Total for Question 3 is 4 marks)

4 $CDEF$ is a quadrilateral.



$$\vec{CD} = \mathbf{a}, \vec{DE} = \mathbf{b} \text{ and } \vec{FC} = \mathbf{a} - \mathbf{b}.$$

- (a) Express \vec{FE} in terms of \mathbf{a} and/or \mathbf{b} .
Give your answer in its simplest form.

.....
(2)

M is the midpoint of DE .
 X is the point on FM such that $FX:XM = n:1$
 CXE is a straight line.

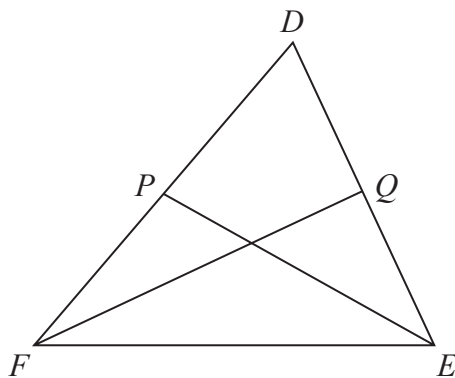
- (b) Work out the value of n .

$$n = \text{.....}$$

(4)

(Total for Question 4 is 6 marks)

5 DEF is a triangle.



P is the midpoint of FD .

Q is the midpoint of DE .

$$\vec{FD} = \mathbf{a} \quad \text{and} \quad \vec{FE} = \mathbf{b}$$

Use a vector method to prove that PQ is parallel to FE .

(Total for Question 5 is 4 marks)

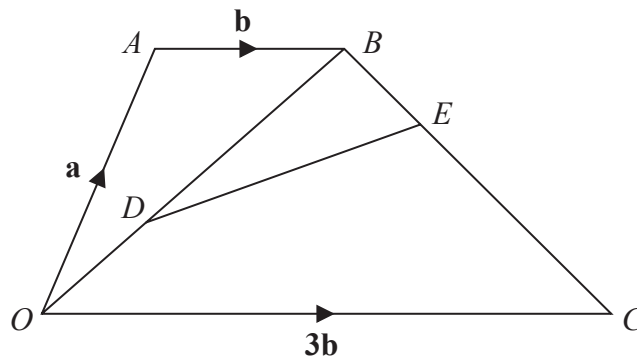
$$6 \quad \mathbf{a} = \begin{pmatrix} 3 \\ 4 \end{pmatrix} \quad \mathbf{b} = \begin{pmatrix} 5 \\ -2 \end{pmatrix}$$

Find $2\mathbf{a} - 3\mathbf{b}$ as a column vector.

$$\begin{pmatrix} \\ \dots \\ \dots \end{pmatrix}$$

(Total for Question 6 is 2 marks)

7 $OABC$ is a trapezium.



$$\vec{OA} = \mathbf{a}$$

$$\vec{AB} = \mathbf{b}$$

$$\vec{OC} = 3\mathbf{b}$$

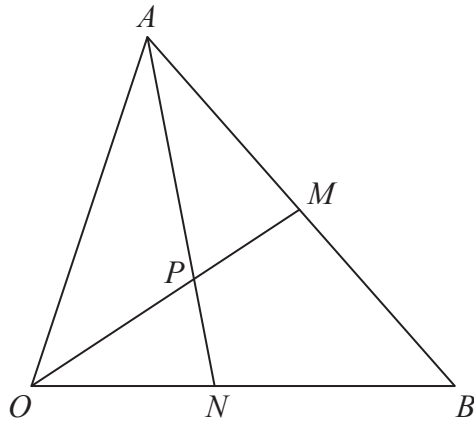
D is the point on OB such that $OD:DB = 2:3$

E is the point on BC such that $BE:EC = 1:4$

Work out the vector \vec{DE} in terms of \mathbf{a} and \mathbf{b} .
Give your answer in its simplest form.

(Total for Question 7 is 4 marks)

8



OAB is a triangle.

OPM and APN are straight lines.

M is the midpoint of AB .

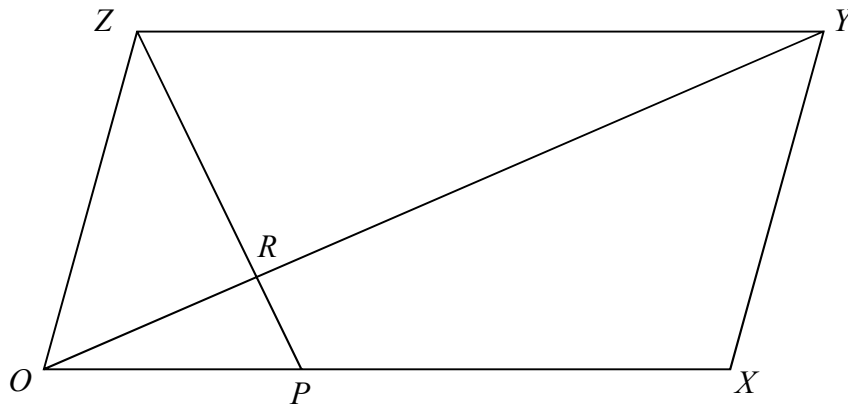
$$\vec{OA} = \mathbf{a} \quad \vec{OB} = \mathbf{b}$$

$$OP:PM = 3:2$$

Work out the ratio $ON:NB$

.....
(Total for Question 8 is 5 marks)

9 $OXYZ$ is a parallelogram.



$$\vec{OX} = \mathbf{a}$$

$$\vec{OY} = \mathbf{b}$$

P is the point on OX such that $OP:PX = 1:2$

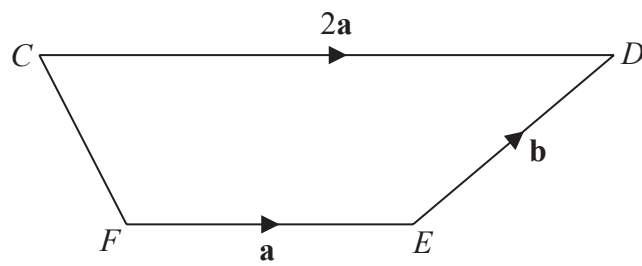
R is the point on OY such that $OR:RY = 1:3$

Work out, in its simplest form, the ratio $ZP:ZR$

You must show all your working.

.....
(Total for Question 9 is 5 marks)

10 $CDEF$ is a quadrilateral.



$$\vec{FE} = \mathbf{a} \quad \vec{ED} = \mathbf{b} \quad \vec{CD} = 2\mathbf{a}$$

The point P is such that CEP is a straight line and that $CE = EP$

Use a vector method to prove that CF is parallel to DP .

(Total for Question 10 is 4 marks)

11 A, B and C are three points such that

$$\vec{AB} = 3\mathbf{a} + 4\mathbf{b}$$

$$\vec{AC} = 15\mathbf{a} + 20\mathbf{b}$$

(a) Prove that A, B and C lie on a straight line.

(2)

D, E and F are three points on a straight line such that

$$\vec{DE} = 3\mathbf{e} + 6\mathbf{f}$$

$$\vec{EF} = -10.5\mathbf{e} - 21\mathbf{f}$$

(b) Find the ratio

length of DF : length of DE

.....
(3)

(Total for Question 11 is 5 marks)

12 **a** and **b** are vectors such that

$$\mathbf{a} = \begin{pmatrix} 2 \\ -3 \end{pmatrix} \quad \text{and} \quad 3\mathbf{a} - 2\mathbf{b} = \begin{pmatrix} 8 \\ -17 \end{pmatrix}$$

Find **b** as a column vector.

$$\begin{pmatrix} \\ \dots\dots\dots \\ \end{pmatrix}$$

(Total for Question 12 is 3 marks)